## LULEÅ UNIVERSITY OF TECHNOLOGY <br> Division of Physics

| Course code | F0047T/MTF107 |
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| Examination date | $2011-03-15$ |
| Time | $09.00-14.00$ (5 hours) |

## Examination in: Kvantfysik / Quantum Physics

Total number of problems: 5
Teacher on duty: Johan Hansson
Examiner: Hans Weber
Tel: 491072, Room E300
Tel: 492088 or 0708-592088, Room E304
Allowed aids: Fysikalia, Physics Handbook, Beta, calculator, Collection of formulae
Define notations and motivate assumptions and approximations. Present the solutions so that they are easy to follow. Maximum number of point is 15 p .7 .0 points are required to pass the examination. Grades 3: 7.0, 4: 9.5, 5: 12.0

## 1. Compton scattering

A $100-\mathrm{keV}$ photon collides with an electron at rest. The photon is scattered through $\theta=90^{\circ}$. (Note, in the figure 1 below the angle is not $90^{\circ}$ )
(a) What is its energy and wavelength of the photon after the collision?
(b) What is the kinetic energy in eV of the electron after the collision?
(c) What is the direction of the recoil (electron)?


Figure 1: Compton scattering of a photon of wavelength $\lambda$ through an angle $\theta$ to a photon of wavelength $\lambda^{\prime}$.

## 2. Angular momentum

For a Nitrogen molecule calculate the change in angular momentum as it emits a photon of wavelength $\lambda=1250 \mu \mathrm{~m}$. The transition is between two close rotational levels. The distance between the Nitrogen atoms in the molecule is $\mathrm{d}=1.094 \AA$. The angular momentum of level $l$ is given by $\sqrt{l(l+1)} \hbar$.

## 3. Spin

Evaluate for a spin $1 / 2$ particle described by the spinor $\chi$ the expectation values of the 3 cartesian components ( $\left.\left.\left\langle S_{x}\right\rangle,<S_{y}\right\rangle,<S_{z}\right\rangle$ ) of the spin and also their squares ( $\left.<S_{x}^{2}\right\rangle$ , $\left\langle S_{y}^{2}\right\rangle,\left\langle S_{z}^{2}\right\rangle$ )

$$
\chi=\frac{1}{3}\binom{2-i}{2} .
$$

## 4. Quantum rotator

The Hamiltonian (in units of eV ) for a given axially symmetric quantum rotator is

$$
\begin{equation*}
H=\frac{L_{x}^{2}+L_{y}^{2}}{3 \hbar^{2}}+\frac{L_{z}^{2}}{4 \hbar^{2}} \tag{3p}
\end{equation*}
$$

What are the possible energies?

## 5. Three-dimensional box well

A particle is placed in the potential (a 3 dimensional box well)

$$
V(x, y, z)=\left\{\begin{array}{cl}
0 & \text { for } \quad 0 \leq x \leq a \text { and } 0 \leq y \leq a \text { and } 0 \leq z \leq \frac{\mathbf{a}}{2} \\
+\infty & \text { for } \quad x>a \text { or } x<0 \text { or } y>a \text { or } y<0 \text { or } z>\frac{\mathbf{a}}{\mathbf{2}} \text { or } z<0
\end{array}\right.
$$

(a) Calculate (solve the Schrödinger equation) the eigenfunctions ?
(b) What are the 7 lowest eigenenergies ?
(c) What are the degeneracies of the states associated to these 7 lowest eigenenergies ?

