

Ex:

$$\frac{\frac{x}{y} + \frac{y}{x} + 2}{\frac{1}{x} + \frac{1}{y}} = \frac{x \cdot y \left( \frac{x}{y} + \frac{y}{x} + 2 \right)}{x \cdot y \left( \frac{1}{x} + \frac{1}{y} \right)} = \frac{\frac{\cancel{x} \cdot \cancel{x} \cdot y}{\cancel{y}} + \frac{\cancel{x} \cdot y \cdot \cancel{y}}{\cancel{x}} + 2 \cdot x \cdot y}{\frac{\cancel{x} \cdot y}{\cancel{x}} + \frac{\cancel{x} \cdot y}{\cancel{y}}}$$

$$= \frac{x^2 + 2 \cdot x \cdot y + y^2}{x + y} = \frac{(x+y)^2}{x+y} = x+y$$


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Ex:

$$\frac{18a^2 + 9ab - 2b^2}{18a^2 + 24ab + 8b^2} - \frac{9b}{2(9a+6b)}$$

$(x+y)^2 = x^2 + 2xy + y^2$

$$18a^2 + 24ab + 8b^2 = 2 \left( \underbrace{9a^2}_{3^2} + \underbrace{12a \cdot b}_{2 \cdot 3 \cdot 2} + \underbrace{4b^2}_{2^2} \right)$$

$$= 2(3a + 2b)^2$$

$$= \frac{18a^2 + 9ab - 2b^2}{2(3a + 2b)^2} - \frac{9b}{2 \cdot 3(3a + 2b)}$$

Mgn:  $2 \cdot 3 \cdot (3a + 2b)^2$

$$= \frac{3(18a^2 + 9ab - 2b^2)}{2 \cdot 3(3a + 2b)^2} - \frac{9b(3a + 2b)}{2 \cdot 3(3a + 2b)^2}$$

$$= \frac{\cancel{3}(18a^2 + \cancel{9ab} - 2b^2 - \cancel{9ab} - 6b^2)}{2 \cdot \cancel{3} \cdot (3a + 2b)^2}$$

$$= \frac{18a^2 - 8b^2}{2(3a + 2b)^2} = \frac{\overset{3^2}{9}a^2 - \overset{2^2}{4}b^2}{(3a + 2b)^2} = \frac{(3a - 2b)(\cancel{3a + 2b})}{(3a + 2b)^2} = \frac{3a - 2b}{3a + 2b}$$

Ex:

$$\frac{2x}{7} = \frac{3}{5}$$

$$\frac{2}{7}x = \frac{3}{5}$$

$$\frac{7}{2} \cdot \frac{2}{7} \cdot x = \frac{7}{2} \cdot \frac{3}{5}$$

$$\frac{7 \cdot 2}{2 \cdot 7} x = \frac{7 \cdot 3}{2 \cdot 5}$$

$$x = \frac{21}{10}$$

Ex:

$$(3x-6)(4x+12) = 0$$

$$3x-6=0 \quad \text{eller} \quad 4x+12=0$$

$$3x=6$$

$$x=2$$

$$4x=-12$$

$$x=-3$$

Ex:

$$4(2x-5)^3 + 7(2x-5)^2 = 0$$

$$(2x-5)^2 (4(2x-5) + 7) = 0$$

$$(2x-5)^2 (8x-20+7) = 0$$

$$(2x-5)^2 (8x-13) = 0$$

$$2x-5=0 \quad \text{eller} \quad 8x-13=0$$

$$2x=5$$

$$x = \frac{5}{2}$$

$$8x=13$$

$$x = \frac{13}{8}$$

$$(x-2)^2 = 0$$

$$x^2 - 4x + 4 = 0$$

$$x=2$$

$$x^2 = 4$$

$$x = 2 \quad \text{oder} \quad x = -2$$

Ex: Rät linje genom  $(1, -2)$  med  $k = -3$

$$y = kx + m$$

$$y = -3x + m$$

gö genom  $(1, -2)$

$$-2 = -3 \cdot 1 + m$$

$$-2 + 3 = m$$

$$m = 1$$

Svar:

$$y = -3x + 1$$

A4

$$y - y_0 = k(x - x_0)$$

$$y - (-2) = (-3)(x - 1)$$

$$y + 2 = (-3)(x - 1)$$

$$y = (-3)x + 3 - 2$$

$$= -3x + 1$$