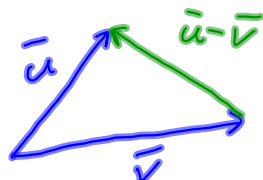
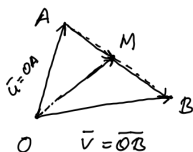


Subtraksiyon mellan vektorer



$$\vec{v} + (\vec{u} - \vec{v}) = \vec{v} + \vec{u} - \vec{v} = \vec{u}$$

Extremal:

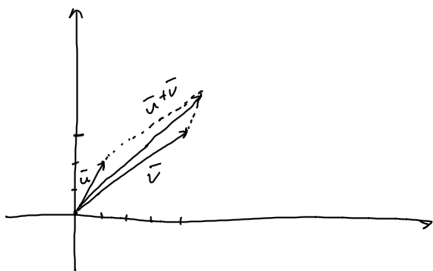


$$\overline{OM} = \overline{OA} + \overline{AM} = \overline{OA} + \frac{1}{2}\overline{AB}$$

$$= \vec{u} + \frac{1}{2}(\vec{v} - \vec{u}) = \vec{u} + \frac{1}{2}\vec{v} - \frac{1}{2}\vec{u}$$

$$= \frac{1}{2}\vec{u} + \frac{1}{2}\vec{v} = \frac{1}{2}(\vec{u} + \vec{v})$$

$$\vec{u} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} \quad \vec{v} = \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$



$$\vec{u} + \vec{v} = \begin{bmatrix} 1 \\ 2 \end{bmatrix} + \begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} 1+4 \\ 2+3 \end{bmatrix} = \begin{bmatrix} 5 \\ 5 \end{bmatrix}$$

$$\begin{aligned} \bullet \quad 2\vec{u} + 3\vec{v} &= 2 \cdot \begin{bmatrix} 1 \\ 2 \end{bmatrix} + 3 \begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} 2 \\ 4 \end{bmatrix} + \begin{bmatrix} 12 \\ 9 \end{bmatrix} \\ &= \begin{bmatrix} 14 \\ 13 \end{bmatrix} \end{aligned}$$

$$\begin{aligned} \bullet \quad |\vec{v}| &= \|\vec{v}\| = \left\| \begin{bmatrix} 4 \\ 3 \end{bmatrix} \right\| = \sqrt{4^2 + 3^2} \\ &= \sqrt{16+9} = \sqrt{25} = 5 \end{aligned}$$

$$\vec{v} = \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} \quad \|\vec{v}\| = |\vec{v}| = \sqrt{v_1^2 + v_2^2}$$

Einheitsvektor mit Richtung \vec{v}

$$\vec{v} = \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$

$$e_{\vec{v}} = \frac{1}{|\vec{v}|} \vec{v} = \frac{1}{5} \begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} 4/5 \\ 3/5 \end{bmatrix}$$