

Department of Mathematics, Luleå University of Technology

M0031M Linjär algebra och differentialekvationer

(Linear Algebra and Differential Equations)

28 Föreläsningar (Lectures) + Lektioner (Exercise Sessions) + 3 MATLAB;

Contact Person: Norbert Euler

Literature:

- 1) D. C. Lay, *Linear Algebra and its Applications*, 3rd Edition 2003
- 2) A. Dunkels at all, *Derivator, integraler och sånt*, Studentlitteratur 2000
- 3) A. Gilat, *MATLAB: an Introduction with Applications*, 3rd Edition. 2008.

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A. Complex Numbers (Dunkels)

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|-----|-------------------------------------------------------------------------------------------------------------------------------------------|-------|
| L1. | Definition of complex numbers and calculation rules (algebraic properties, conjugate number, modulus=absolute value, triangle inequality) | 9.1-2 |
| L2. | Polar form of complex numbers and de Moivre formula | 9.3-4 |
| L3. | Algebraic equations (quadratic equations, polynomials and algebraic equations) | 9.5-6 |
| L4. | Equation $z^n = w$ and function e^z | 9.7-8 |
| L5. | Reserve | |

B. Linear Algebra (Lay)

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| L6. | Vector spaces and subspaces | 4.1 |
| L7. | Null spaces, column spaces, and linear transformations | 4.2 |
| L8. | Linearly independent sets. Bases | 4.3 |
| L9. | Coordinate system | 4.4 |
| L10. | The dimension of a vector space. Rank | 4.5-6 |
| L11. | Change of basis | 4.7 |
| L12. | Eigenvectors and eigenvalues. The characteristic equation | 5.1-2 |
| L13. | Diagonalization, eigenvectors and linear transformations | 5.3-4 |
| L14. | Inner product, length. Orthogonality and orthogonal sets | 6.1-2 |
| L15. | Orthogonal projections. The Gram-Schmidt process | 6.3-4 |
| L16. | Least-squares problems | 6.5-6 |
| L17. | Inner product spaces | 6.7 |
| L18. | Diagonalization of symmetric matrices | 7.1 |
| L19-20. | Reserve | |

C. Differential Equations (Dunkels)

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| L21. | Introduction to differential equations and linear differential equations | 10.1-5 |
| L22. | Linear differential equations of first order (method of variation of constant; separable equation) | 10.6-7 |
| L23. | Homogeneous differential equations of the second order | 10.8 |

L24. Nonhomogeneous differential equations of the second order	10.8-9
L25. Variation of parameters	10.10
L26. Euler differential equation	10.11-12
L27. Linear differential equations of higher order	10.13

D. Repetition

L28. Repetition



G. M0031M – Exercises = 14

Complex Numbers (Dunkels book)

- 9.11.1:** 9.1acg, 9.2b, 9.3a, 9.4, 9.6, 9.7, 9.9, 9.11, 9.13 (9.1bd, 9.2a, 9.3b, 9.4c, 9.8, 9.12)
- 9.11.2:** 9.16abe, 9.17, 9.18, 9.20, 9.21 (9.16cf, 9.22)
- 9.11.3:** 9.25a, 9.29, 9.30acef (9.25b, 9.26, 9.30dg)
- 9.11.4:** 9.32ac, 9.33, 9.34, 9.35, 9.36, 9.37, 9.39acd, 9.41, 9.44ac, 9.45ab, 9.46, 9.50
(9.32b, 9.38, 9.39b, 9.42, 9.44b, 9.45c, 9.47, 9.48)

Linear Algebra (Lay book)

- 4.1:** 1, 3, 5, 9, 12, 15, 21 (7, 10, 13, 18, 22)
- 4.2:** 1, 3, 5, 7, 9, 15, 17, 19, 21, 23, 25, 28, 31, 33 (2, 4, 8, 11, 16, 18, 22, 24, 32)
- 4.3:** 1, 3, 5, 9, 11, 13, 15, 19, 26, 31, 33 (7, 16, 23, 25, 32, 34)
- 4.4:** 1, 3, 5, 9, 10, 11, 13, 17, 21, 27, 32 (4, 7, 12, 14, 22, 31)
- 4.5:** 1, 3, 7, 11, 13, 15, 21, 23, 27 (5, 9, 16, 19, 22, 25)
- 4.6:** 1, 4, 5, 7, 8, 9, 25, 28, 29, 32 (3, 6, 11, 13, 17, 21, 27)
- 4.7:** 1, 3, 5, 7, 13 (2, 6, 8, 11, 14)
- 5.1:** 1, 3, 5, 7, 10, 13, 17, 19, 25, 26, 31 (4, 8, 14, 21, 23, 32)
- 5.2:** 1, 9, 15, 18, 20, 23, 24 (3, 11, 17, 21)
- 5.3:** 1, 3, 5, 7, 13, 19, 23, 31 (4, 9, 11, 17, 24, 25, 32)
- 5.4:** 1, 3, 5, 7, 9, 11, 15, 17, 20, 25, 29 (2, 4, 6, 10, 13, 21, 27)
- 6.1:** 1, 3, 5, 7, 11, 13, 16, 17, 22, 24, 25, 28, 31 (12, 14, 15, 23, 27, 29)
- 6.2:** 1, 5, 7, 9, 11, 13, 15, 17, 21, 26-30 (3, 10, 12, 14, 16, 20, 32)
- 6.3:** 1, 3, 7, 9, 11, 13, 15, 17, 19, 24 (2, 5, 10, 12, 14, 18)
- 6.4:** 3, 4, 6, 11, 22 (2, 9, 16, 17)
- 6.5:** 3, 5, 9, 13, 15, 19, 20, 25 (4, 6, 11, 14, 16, 24)
- 6.6:** 1, 2, 3, 4, 7, 8
- 6.7:** 1, 3, 5, 9, 12, 14, 18, 21, 23, 25 (2, 4, 6, 13, 17, 22, 24, 26)
- 7.1:** 1-6, 8, 13, 17, 19, 21, 23, 28, 30 (11, 22, 24)

Differential Equations (Dunkels book)

10.14.1: 10.1, 10.3, 10.5 (10.6)

10.14.3: 10.15abde, 10.16acde, 10.19, 10.20

10.14.4: 10.28, 10.29abcd, 10.30, 10.31 (10.29e)

10.14.5: 10.40, 10.41c, 10.43, 10.44, 10.46-48, 10.50-51, 10.53, 10.57 (10.41b, 10.43, 10.54)

10.14.7: 10.60ad, 10.61, 10.63 (10.60e, 10.62)

10.14.8: 10.65, 10.66, 10.72, 10.74, 10.81, 10.84, 10.85, 10.86, 10.87, 10.88 (10.67, 10.69, 10.76, 10.93)

MATLAB Exercises (3rd edition of Gilant)

Lab 1:

1.10: 1, 2, 4, 5, 6, 16

2.11: 1, 4, 14

Lab 2:

3.9: 7, 9, 18

6.13: 3, 5, 6, 13

Lab 3:

10.6: 12, 14, 15, 19, 20, 21

11.10: 14, 16